

CT Physics

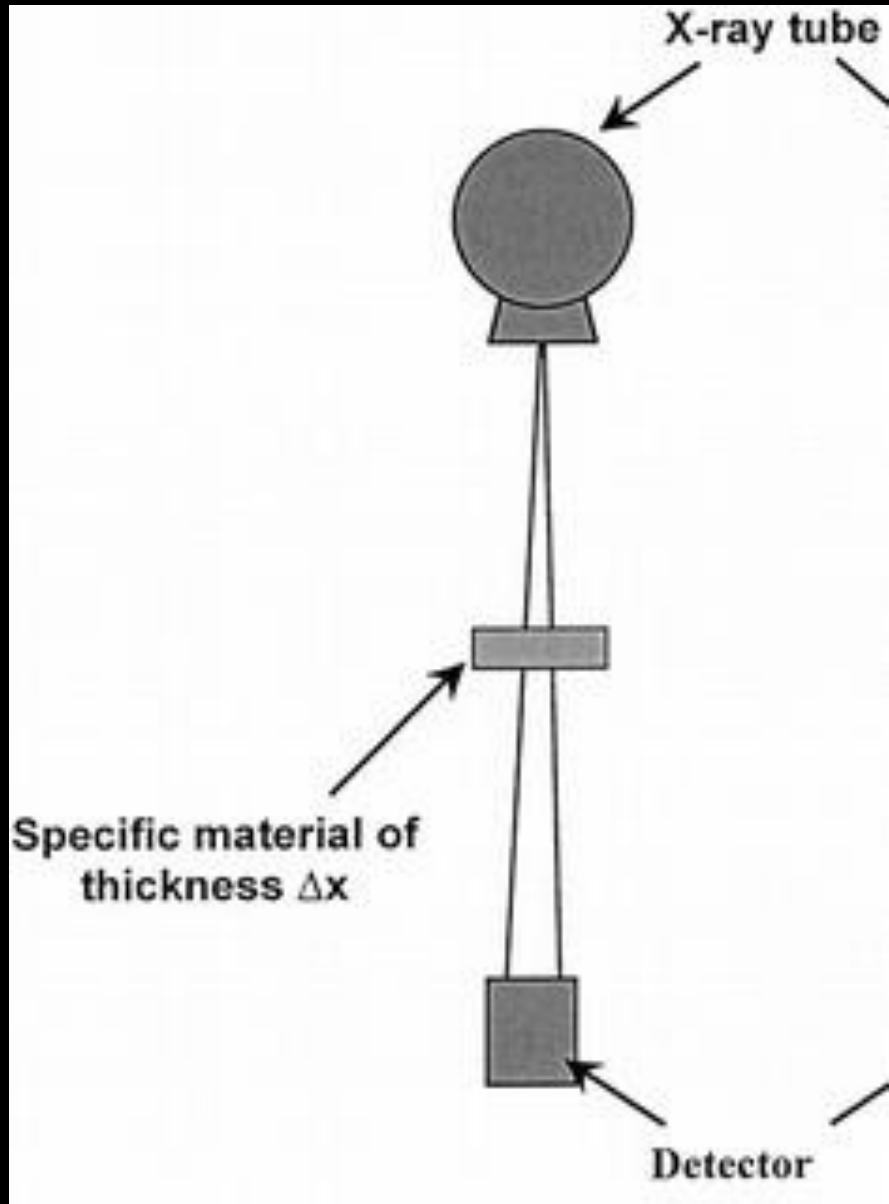
Brant and Helms 2018

Clare Poynton, MD, PhD

Outline

- Acquisition and Reconstruction
- Hounsfield units
- Image Display (windows and levels)
- Artifacts

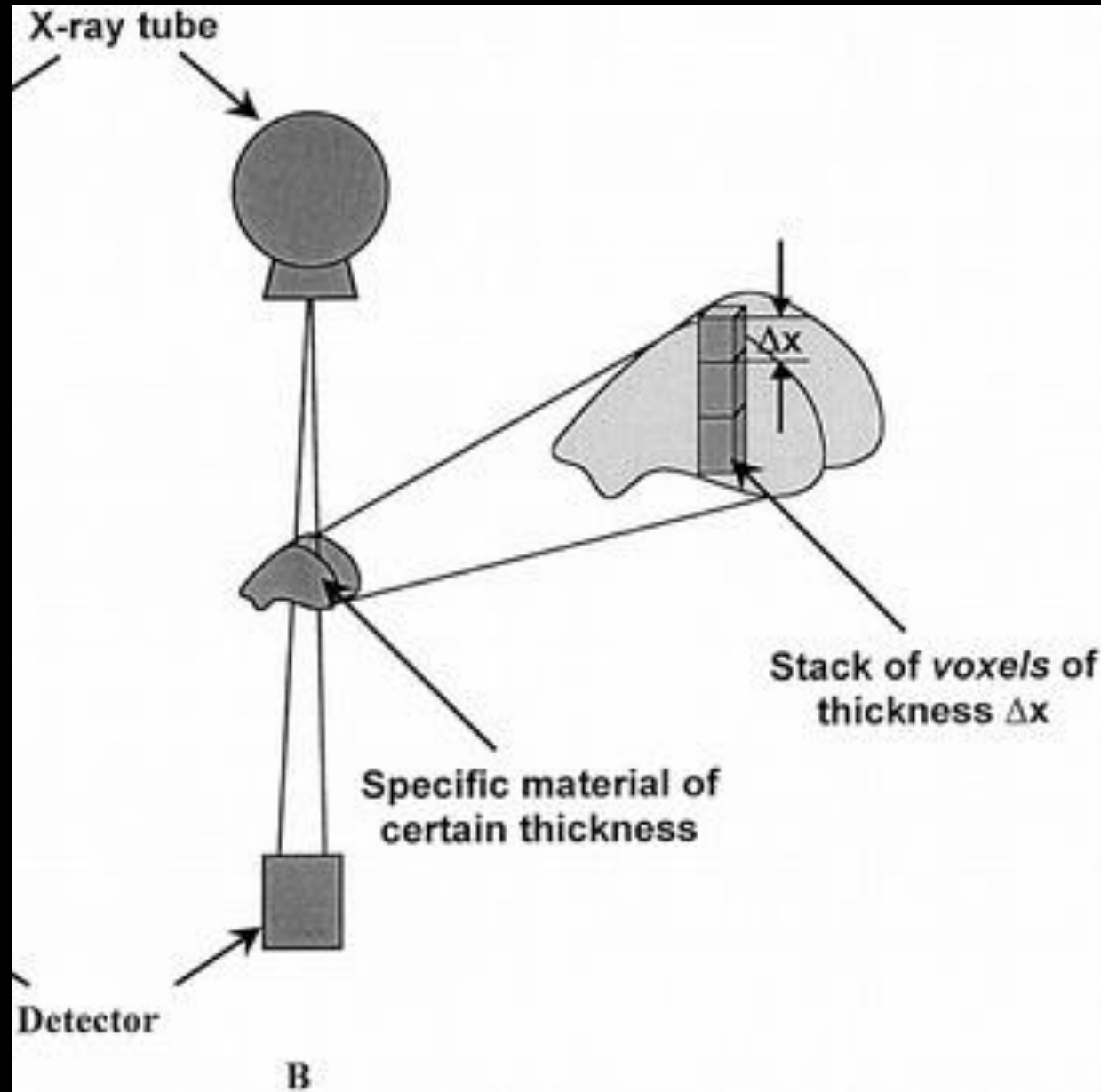
Acquisition



$$I_t = I_o e^{-\mu \Delta x}$$

- I_t is the x-ray intensity measured at the Detector
 - I_o is the x-ray intensity at the source
 - Δx is the thickness
 - μ is the UNKNOWN linear attenuation coefficient of the material
- Solve for μ

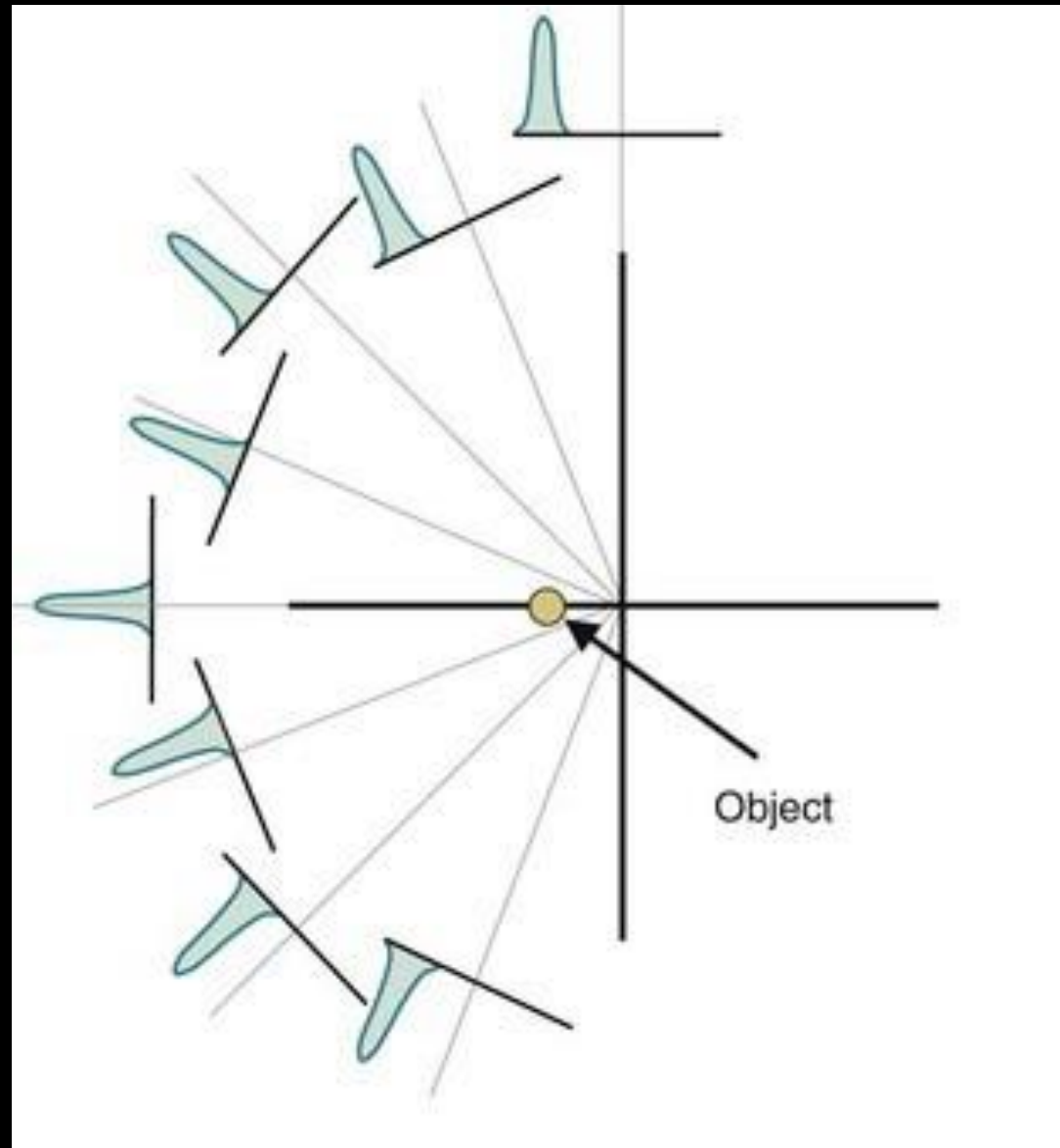
Acquisition



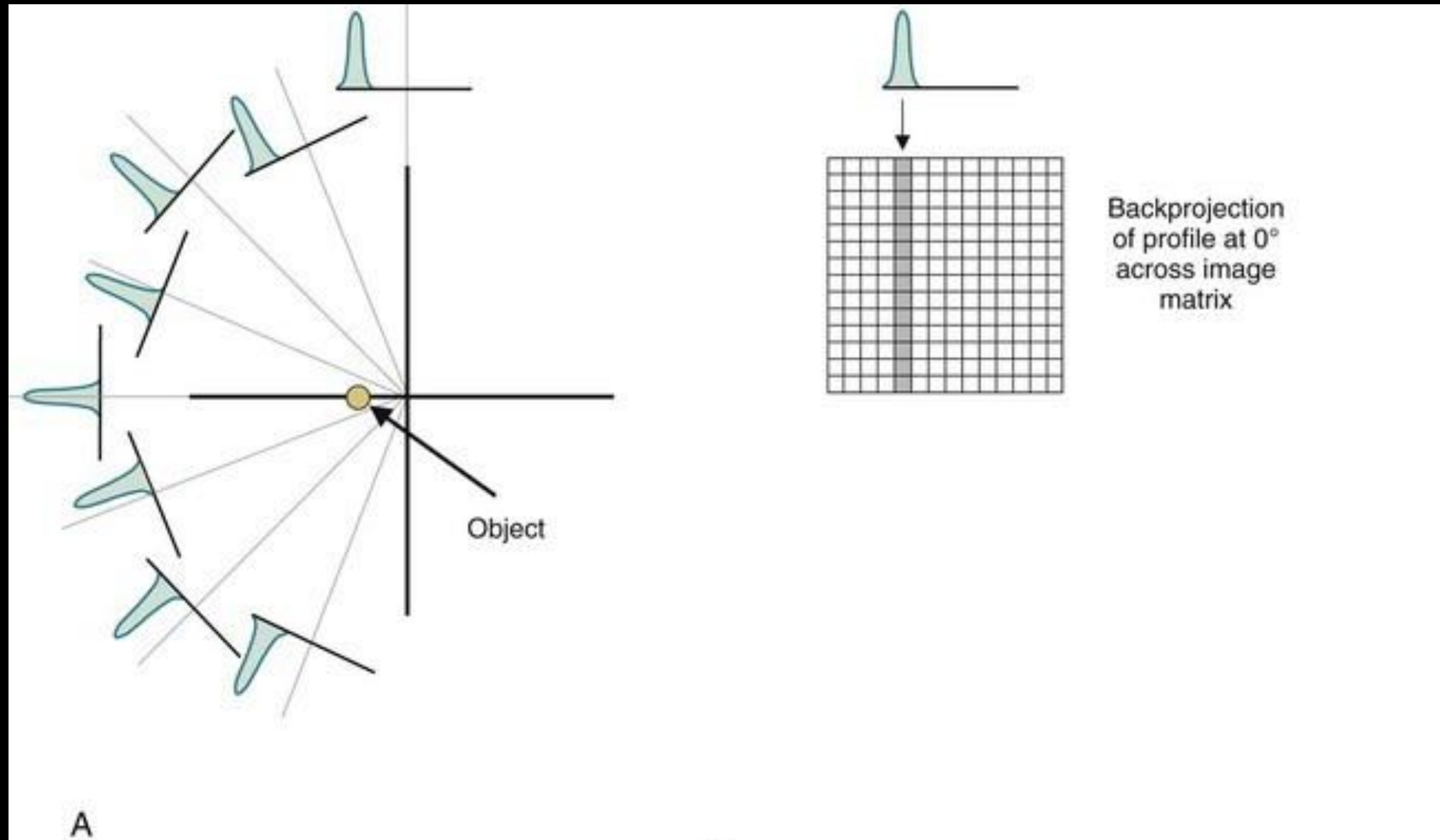
$$I_t = I_o e^{-\sum_{i=1}^k \mu_i \Delta x}$$

- In reality, our xray passes through multiple voxels each with an unknown μ_i
- Now we have 1 equation and multiple unknown variables, μ_i
→ cannot solve

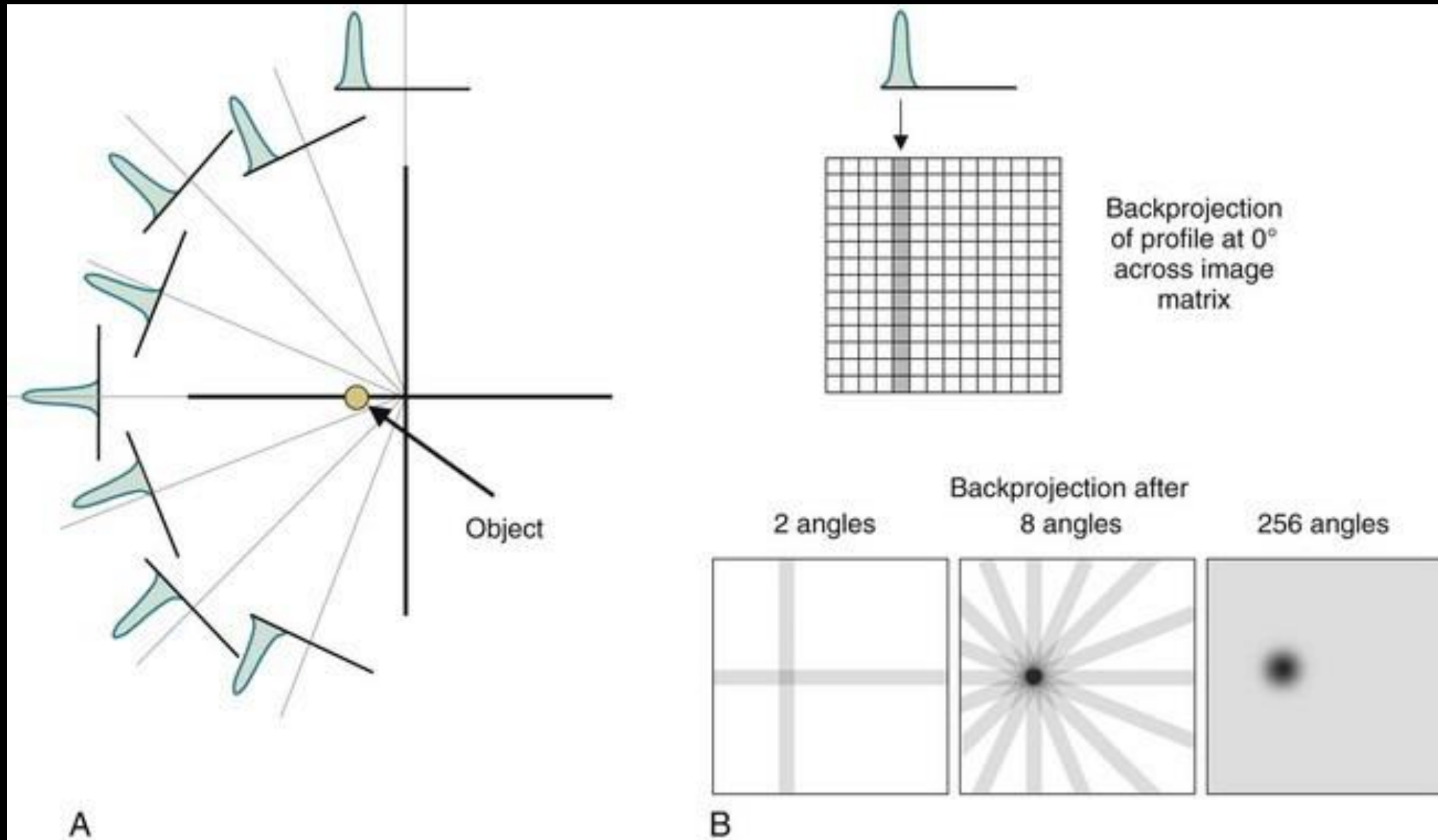
Acquisition: multiple projections



Reconstruction: Filtered Back Projection



Reconstruction: Filtered Back Projection



Reconstruction: Filtered Back Projection

- What does “Filtered” refer to in Filtered Back Projection?

Reconstruction: Filtered Back Projection

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- Projection data are multiplied by a mathematical reconstruction filter (MRF) prior to back projection

Reconstruction: Filtered Backprojection

- What does “Filtered” refer to in Filtered Backprojection?
- Projection data are multiplied by a mathematical reconstruction filter (MRF) prior to back projection
- Different filters (MRF) can be applied
 - ‘sharpen’ the image (ie. Bone)
 - ‘smooth’ the image (ie. Soft tissue)

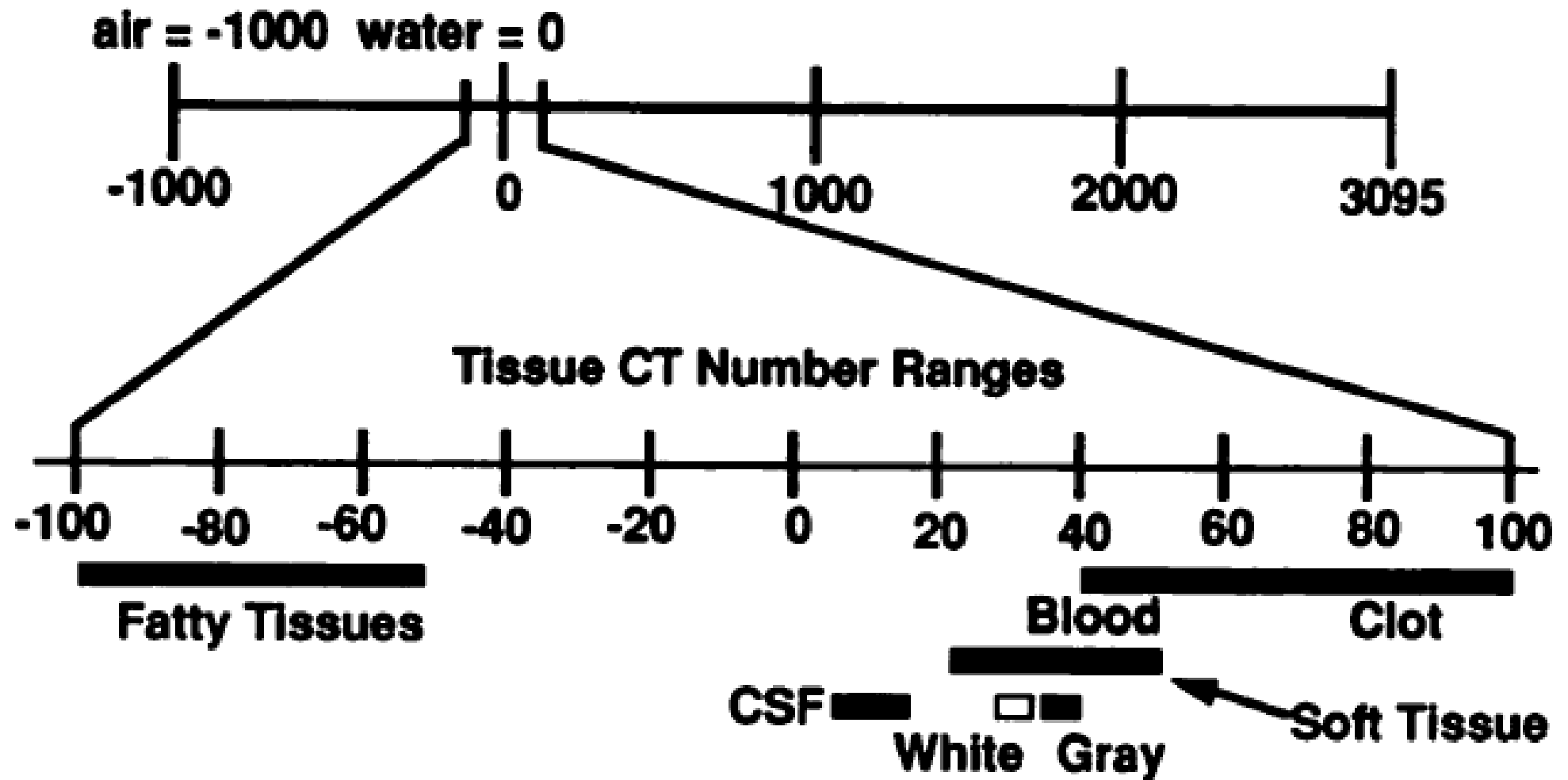
Reconstruction: Hounsfield units

- The result of filtered back projection is a map of estimated attenuation values
- These values are scaled to produce Hounsfield units
- Hounsfield unit = $(\mu_i - \mu_w) * F$
 - μ_i is the attenuation of the material of interest in a voxel
 - μ_w is the attenuation of water
 - F is a scaling factor
- Hounsfield units are also called “relative attenuation values” or “CT numbers”

Hounsfield units

- Water = 0
- Air = -1000
- At 120 keV:
 - Fat \approx -100
 - Soft tissue \approx 50
 - Bone $>$ 1000

CT Numbers Hounsfield Scale



Hounsfield units (HU) vary with acquisition and reconstruction parameters

- HU depend on attenuation coefficients, μ

recall:
$$\text{HU} = (\mu_i - \mu_w) * F$$

Hounsfield units (HU) vary with acquisition and reconstruction parameters

- HU depend attenuation coefficients, μ

recall:
$$HU = (\mu_i - \mu_w) * F$$

- The attenuation of the xray depends the material, but also on KeV

Hounsfield units (HU) vary with acquisition and reconstruction parameters

- HU depend on Attenuation coefficients, μ

recall:
$$HU = (\mu_i - \mu_w) * F$$

- Attenuation coefficients depend on the material, but also on KeV
- keV (kiloelectron volts) – voltage. Can think of this as the photon energy of the xrays

Hounsfield units (HU) vary with acquisition and reconstruction parameters

Photon Energy	Photon Energy (keV)			
	40	50	60 ^a	80
Fat	-150	-110	-90	-70
Soft tissue	60	56	53	50
Cortical bone	3,800	2,600	4,000	2,100
Dilute iodine ^b	400	300	200	100

^aAverage energy expected for CT spectra obtained at 120 kV.

^bObtained by dividing the computed iodine HU by 1,000.

- Chart shows HU for different materials at different keV

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- Lower keV → Increases Contrast of the image

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- Lower keV → reduces radiation dose

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- Lower keV → less penetration (bad for larger patients)

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- kVp (peak keV of xray beam) is usually 80 - 140 keV

Hounsfield units (HU) vary with acquisition and reconstruction parameters

- Acquisition

- keV

Lower keV → Increases Contrast of the image

- Resolution

Larger voxels → more partial volume effects
(ie. voxel more likely to contain mix of fluid, soft tissue)

Voxel size (mm) = FOV (mm) / Matrix size (unit less)

Hounsfield units (HU) vary with acquisition and reconstruction parameters

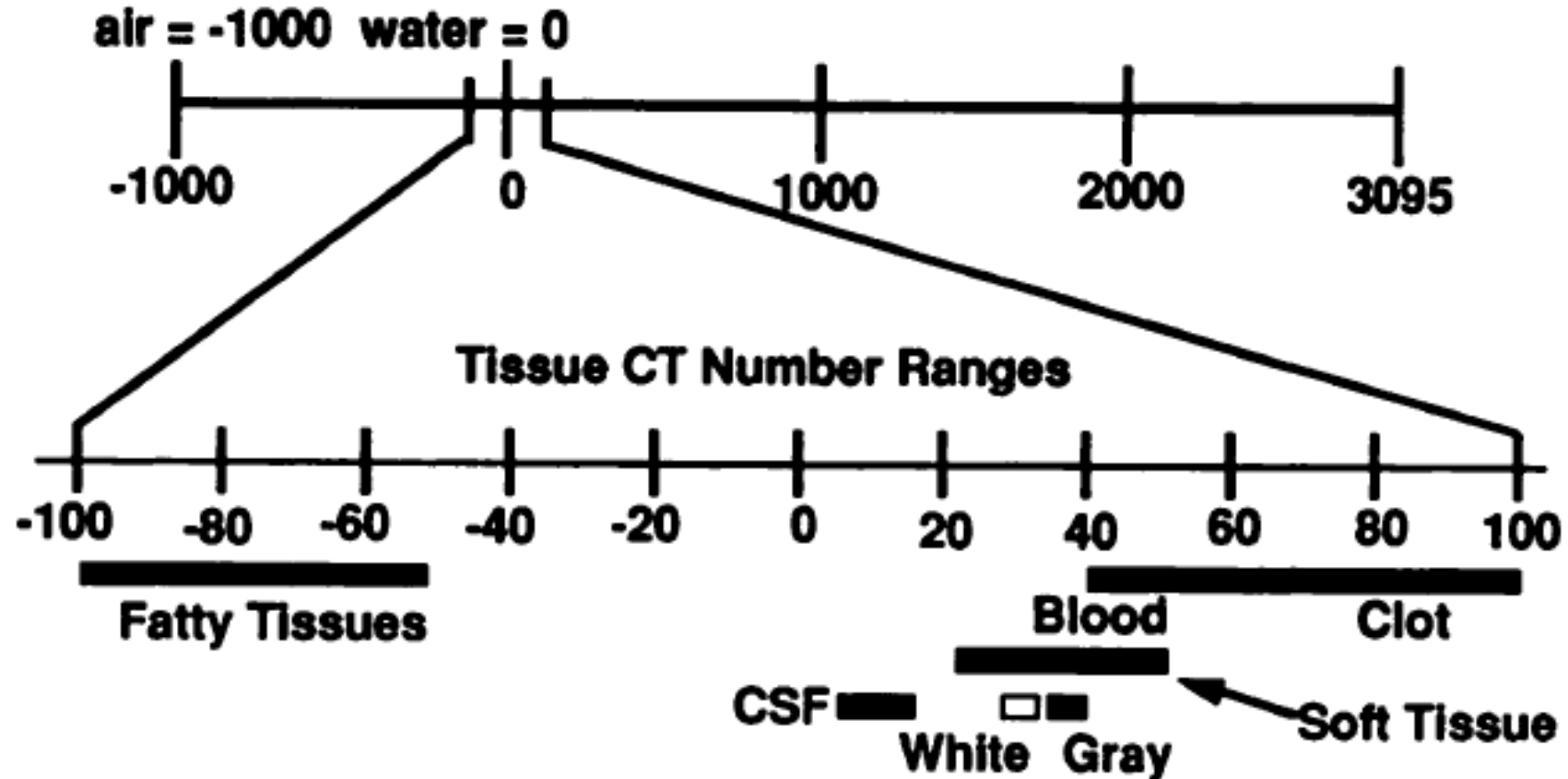
- Acquisition
 - keV
 - *Resolution (partial volume effects) – practical consideration, not test answer*
“Too small to characterize, but likely a benign cyst”
- Reconstruction
 - Filtering that’s done during Filtered Back Projection

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 - Image Display (windows and levels)
- Artifacts

Image Display : Windows and Levels

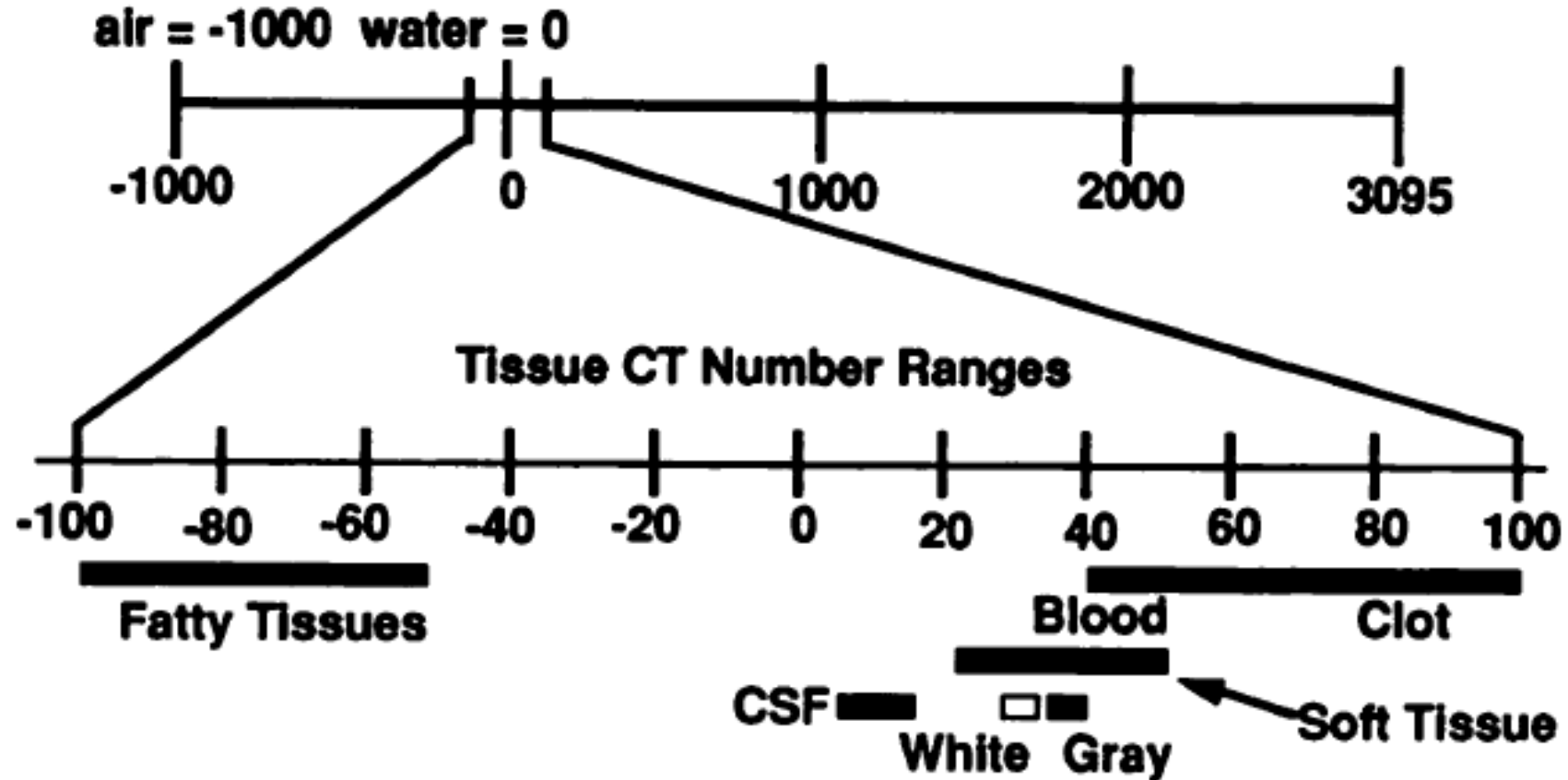
CT Numbers Hounsfield Scale



Range of possible HU = 4096 = 2^{12} (12 bits of memory allocated)

Image Display : Windows and Levels

CT Numbers Hounsfield Scale

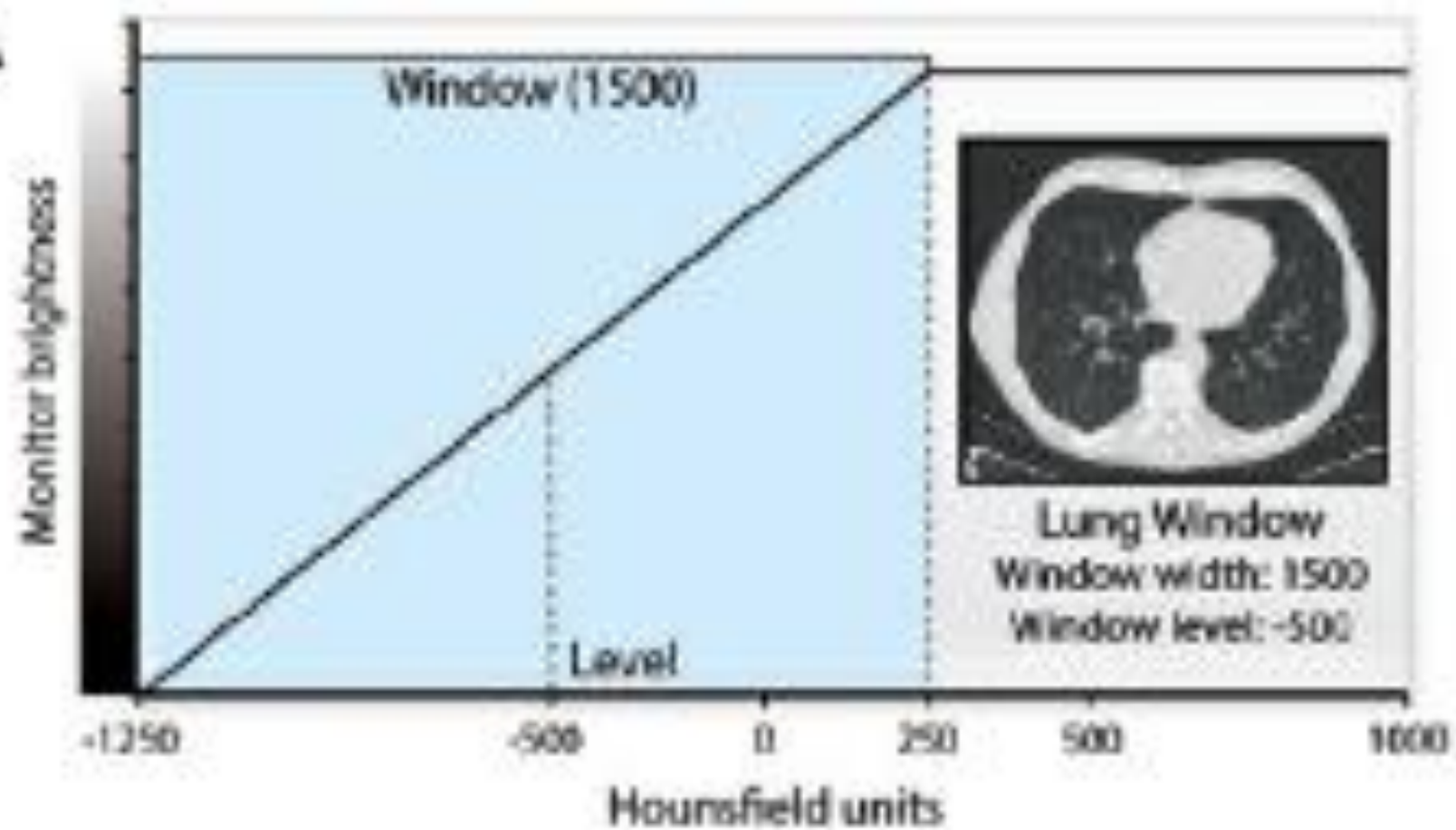


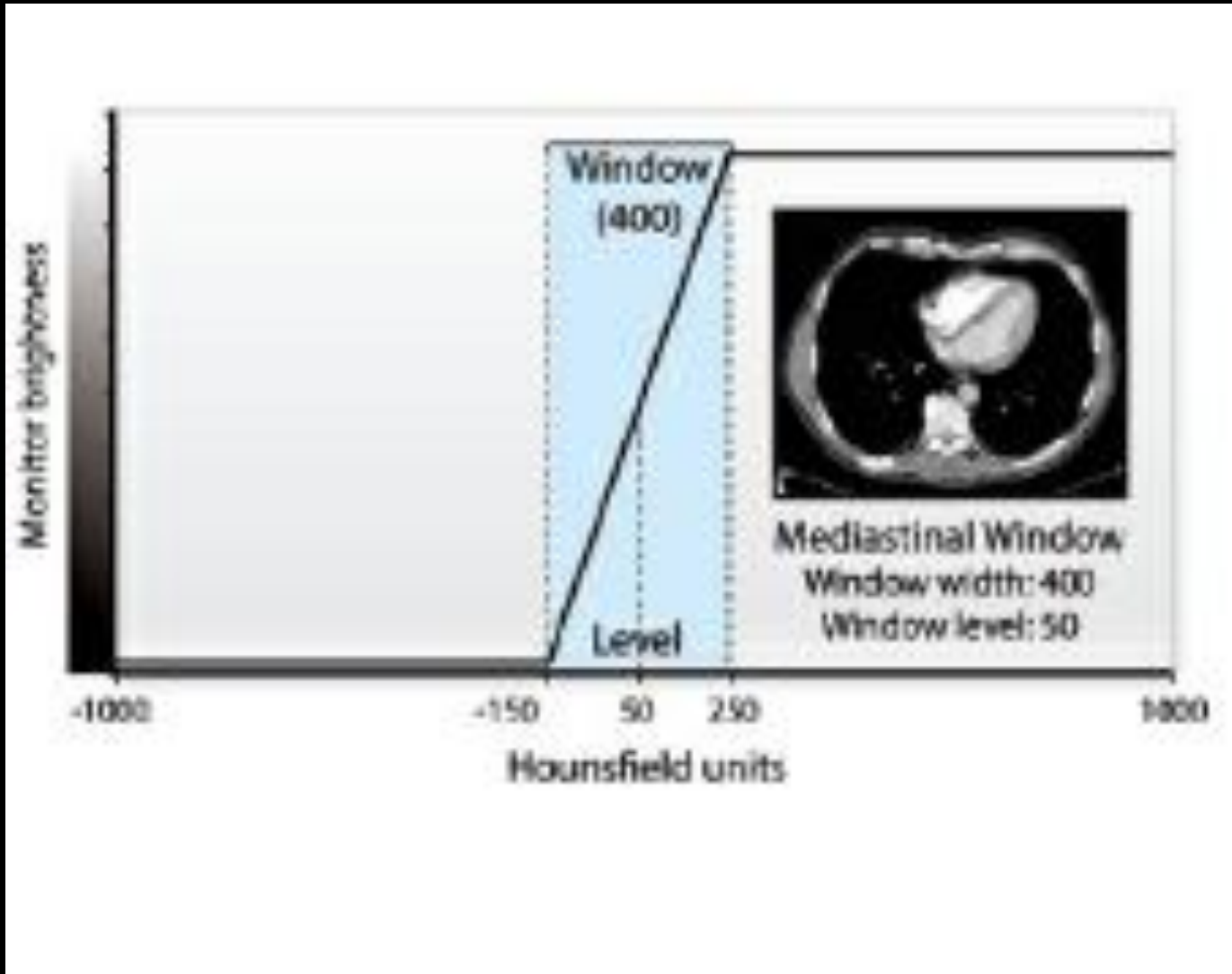
Human visual system cannot perceive 4096 shades of grey

Image Display : Windows and Levels

- Window
 - defines the range of HU that are mapped to displayed grayscale values
- Level
 - defines the center of that range

A



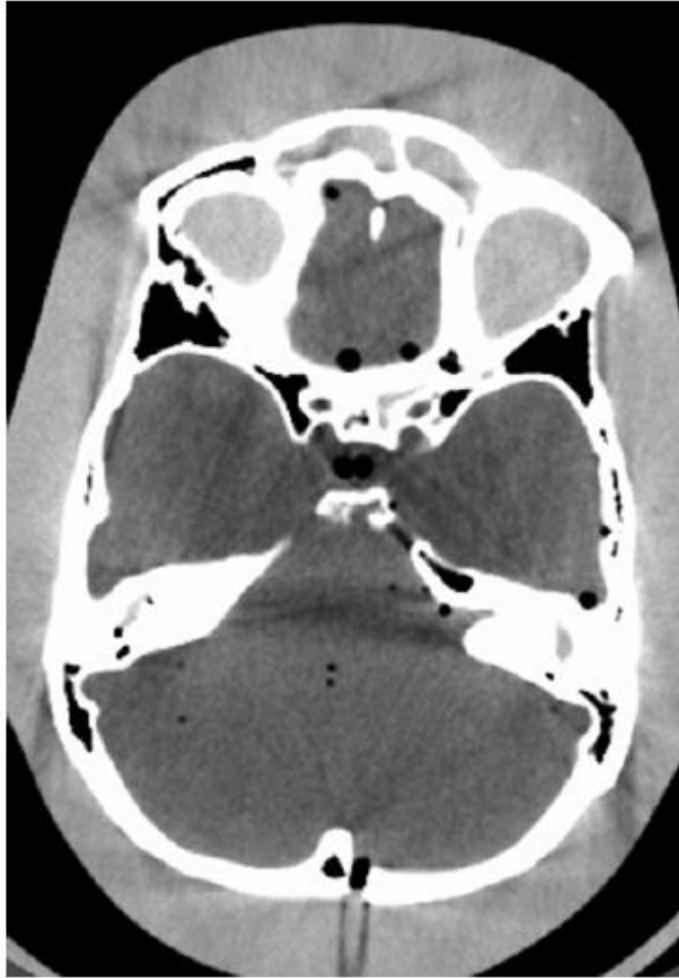


- Decreasing (narrowing) the window width → increases contrast
- Decreasing the level → increases brightness of image

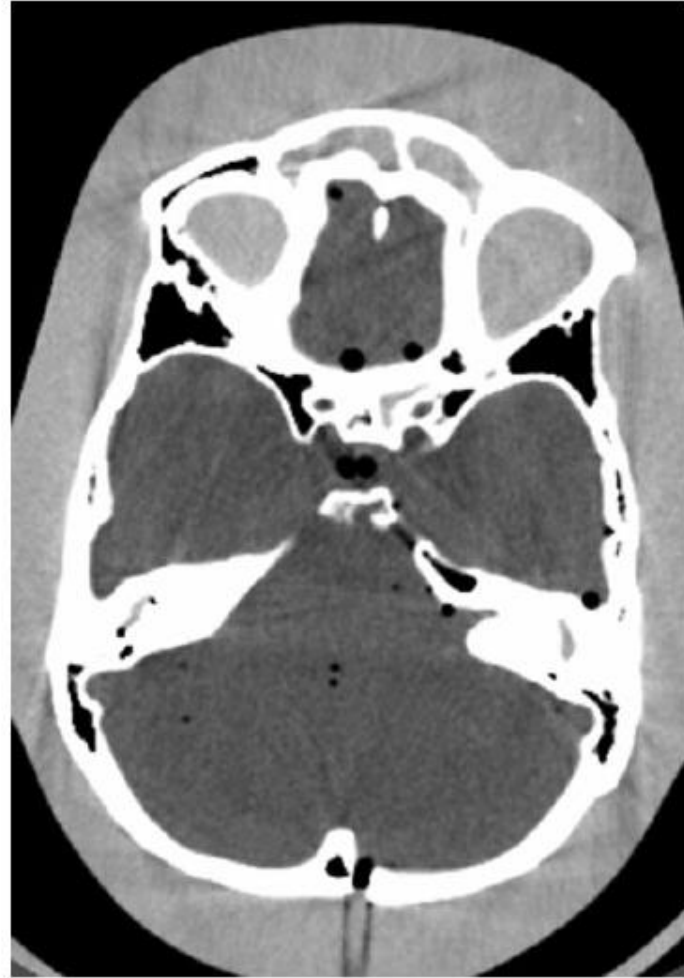
Common Artifacts

- Beam Hardening
- Streak artifact
- Motion artifact

Beam Hardening



a.



b.

Streak and motion artifacts



References

- Huda, W. Review of Radiologic Physics, 4th ed. Lippincott Williams & Wilkins, Jan 20, 2016.
- Barnes, J. Radiographics. 1992. 12:825-837.
- Barrett, J, et al. Radiographics 2004; 24:1679–1691.
- Siegel MJ, et al. Radiology. 2004 Nov;233(2):515-22.